

SURGE INSTABILITY ON A CAVITATING PROPELLER

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Abstract

This study details experiments investigating a previously unrecognized surge instability on a cavitating propeller in a water tunnel. The surge instability is first explored through visual observation of the cavitation on the propeller blades and in the tip vortices. Similarities between the instability and previously documented cavitation phenomena are noted. Measurements of the radiated pressure are then obtained, and the acoustic signature of the instability is identified. The magnitudes of the fluctuating pressures are very large, presumably capable of producing severe hull vibration on a ship.

The origins of the instability are explored through separate investigation of the cavitation dynamics and the response of the water tunnel to volumetric displacement in the working section. Experiments are conducted to quantify the dynamics of the propeller cavitation. Finally, a model is developed for the complete system, incorporating both the cavitation and facility dynamics. The model predicts active system dynamics (linked to the mass flow gain factor familiar in the context of pump dynamics) and therefore potentially unstable behavior for two distinct frequency ranges, one of which appears to be responsible for the instability.

1 Introduction

Experimental experience and theoretical analyses have revealed that the adverse effects of cavitation are often augmented under unsteady flow conditions. The fluctuations of the cavitation volume on a ship's propeller, for example, can cause severe and often structurally damaging vibrations to the hull at the aft end of a ship. Because of this and related problems in pumps, turbines, and other potentially cavitating devices, there is a clear need to understand unsteady phenomena and instabilities connected to cavitating flows.

One such phenomenon is the partial cavity instability on a single hydrofoil or cascade of hydrofoils (Wade and Acosta 1966, Franc and Michel 1988, Le *et al.* 1993, de Lange *et al.* 1994). The behavior of hydrofoils subject to forced oscillation in pitch about a spanwise axis has also been the subject of much research. Many investigators (Shen and Peterson 1978, Franc and Michel 1988, Hart *et al.* 1990, McKenney and Brennen 1994, Reisman *et al.* 1998) have examined the periodic formation and collapse of clouds of cavitation bubbles on the suction surface of hydrofoils and the very large transient pressure pulses and severe structural damage that can result.

Implicitly assumed in many of these investigations is that the phenomena observed within the laboratory facilities accurately reflect the cavitation behavior of devices operating in more open conditions. Only a few studies (Shen and Peterson 1978, Kjeldsen *et al.* 1999) have considered the interactions between the dynamics of the unsteady cavitation and the dynamics of the surrounding experimental facility.

This is not the case for cavitating pumps, where for some time the dynamics of the pump cavitation and the response of the surrounding facility have been known to interact with very dramatic consequences, including the catastrophic POGO instability observed in liquid-propelled rockets. A great deal of research has therefore been focused on quantifying the cavitation dynamics involved in oscillations of this nature. A relatively consistent approach has been adopted, with efforts aimed at developing a transfer matrix characterizing the relationship between the fluctuating pressure and mass flow rate at the pump inlet and the same

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quantities at discharge. The transfer matrix summarizes the dynamic behavior of the pump, including the cavitation. In determining the elements of this transfer matrix, two important parameters were identified. The cavitation compliance models the effective compressibility of the cavitating flow between the inlet and outlet (Brennen and Acosta 1973) and was shown to play an important role in several observed hydraulic system instabilities. A second factor, the mass flow gain factor, represents the response of the cavitation to variations in the inlet mass flow rate (Brennen and Acosta 1976). It was later demonstrated (Brennen 1978, Tsujimoto *et al.* 1993) that this parameter, for which a typically positive value implies an increase in cavitation volume with decreasing inlet mass flow rate, is a key factor in sustaining instabilities in cavitating pumps. One such instability is the “auto-oscillation” of cavitating inducers (Braisted and Brennen 1978, 1980), in recent years renamed cavitation surge. The first attempts to experimentally measure the mass flow gain factor as well as the cavitation compliance and the other components of the transfer matrix were performed by Ng and Brennen (1978), with more precise measurements later obtained by Brennen *et al.* (1982). More recently, the frequency dependence of the mass flow gain factor has been explored theoretically by Otsuka *et al.* (1996).

The majority of investigations exploring the unsteady cavitating behavior of propellers has focused on the consequences of the varying inflow encountered by a propeller blade as it rotates through the irregular wake behind a ship hull. Huse (1972) was the first to explore the resulting variations in cavity volume and their effect on the pressures radiated by the cavitation. The amplitude of the pressure fluctuations and the induced vibrations of the ship hull were found to be orders of magnitude greater than for the case of steady cavitating flow. An excellent summary of the large body of work focused on the propeller-hull vibration problem is offered in Weitendorf (1989). A discussion of the various unsteady cavitation structures that can result from the irregular wake is presented by Bark (1986). McKenney (1995) explored the unsteady flow field encountered by a yawed propeller and its effect on tip vortex cavitation.

Few if any cavitating propeller investigations have adopted an approach similar to the cavitating pump analyses and explored the possible interaction between unsteady propeller cavitation and the dynamics of the surrounding environment. The goal of this work is to utilize concepts garnered from general unsteady cavitation research and extend several more specific concepts from investigations of cavitating pump instabilities to describe and explain a previously unobserved cavitation surge instability on a propeller.

2 Propeller Cavitation Surge Observations

A 190.5 *mm* diameter model propeller typical of the modern designs used by the U.S. Navy was installed in the Low Turbulence Water Tunnel (LTWT) at Caltech (Gates 1977) using a transverse shaft and gear box taken from an outboard motor (McKenney 1995). The fairing around the shaft and gearbox was quite streamlined. The entire assembly could be rotated about its base so as to operate the propeller either upstream of downstream of the fairing.

Experiments began with the propeller mounted upstream of the fairing. Later, when the propeller was operated downstream of the fairing, a violent surge instability was observed to occur in certain regimes of operation. The instability was characterized by a periodic increase and decrease in the extent of cavitation both on the propeller blades and in the tip vortices shed downstream. This fluctuation in cavitation extent was readily apparent to the naked eye, and occurred evenly and synchronously on all blades and at all angular locations. The resulting pressure fluctuations were dramatic, easily audible to the unaided ear, and propagated throughout the experimental facility. The instability was observed across the range of propeller rotation speeds at which the cavitating conditions could be achieved, $n = 28.3 - 31.7 \text{ Hz}$. The frequency of the fluctuation was repeatable and in the range $f = 9 - 11 \text{ Hz}$. The variation of the fluctuation frequency with the basic flow parameters is discussed in greater detail in Duttweiler (2001).

Figure 1 presents selected frames from high speed video footage of the instability on the cavitating propeller. The number indicated in each frame corresponds to the fraction, τ , of the instability cycle elapsed. The beginning of the instability cycle is chosen arbitrarily to coincide with the minimum cavitation extent. This condition, as seen in the first frame of Figure 1, is characterized by a relatively small region of bubbly cavitation along the leading edge of the propeller blade.

Further into the instability cycle, at $\tau = 0.25$, the cavity has grown substantially towards the trailing edge of the propeller blade. A re-entrant jet becomes distinguishable as it is swept back from the leading edge,

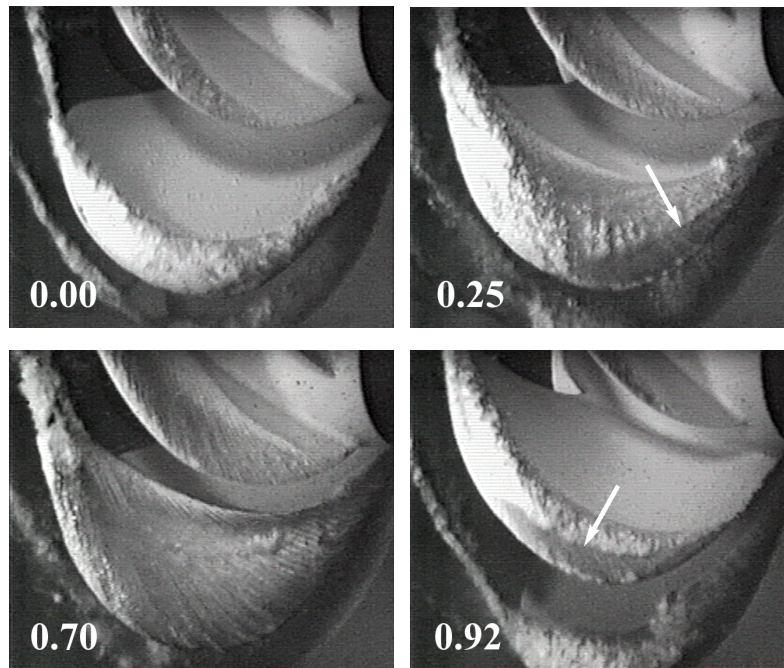


Figure 1: Four frames taken from a high speed video, showing the variation in cavitation on an individual propeller blade during the instability cycle. The number in the lower left corner of each frame, τ , indicates the fraction of the instability cycle elapsed. The white arrow indicates the front of the re-entrant jet.

its forward front indicated by the white arrow. The cavity reaches its maximum extent at approximately $\tau = 0.70$. At this stage of the instability cycle, a supercavitating condition occurs when the cavity near the tip of the propeller blade extends downstream of the trailing edge of the blade. As this cavitation is entrained into the tip vortices it leads to a readily observed increase in the diameter of the vortices shed downstream of the propeller. No re-entrant jet is visible at this point in the cycle, presumably because the jet fluid has been swept past the cavity closure region.

By $\tau = 0.92$ the cavitation has begun to decrease in extent, receding towards the leading edge of the propeller blades. The re-entrant jet can again be observed, indicated by the white arrow, as it begins its rush forward within the cavity towards the leading edge of the propeller. When the re-entrant jet reaches the leading edge at nearly all spanwise locations, the cavitation returns to the minimal configuration shown at $\tau = 0.00$.

While no record of an instability of this nature could be found in the literature, it is evident from Figure 1 that there are similarities between the instability cycle and the well documented partial cavity instability observed on two-dimensional hydrofoils (Wade and Acosta 1966, Franc and Michel 1988, Le *et al.* 1993, deLange *et al.* 1994). First, the cavity length on the propeller blade is fluctuating between two very different but consistent values. Furthermore, the cavity lengths about which the fluctuation occurs are comparable to the chord length, c , of the propeller blade. Finally, the frequency, f , of the fluctuation is quite low. Wade and Acosta (1966) reported reduced frequencies, $k = fc/U$, based on chord length and incoming flow velocity, U , in the range $k = 0.07 - 0.14$. Le *et al.* (1993) and de Lange *et al.* (1994) encountered somewhat higher values of approximately $k = 0.34$. If reduced frequencies for the propeller based on chord length and incident velocity are computed at various radii, values of the order of $k = 0.07$ are obtained. These are consistent with the range reported by Wade and Acosta (1966), but somewhat lower than the value reported by the other investigators.

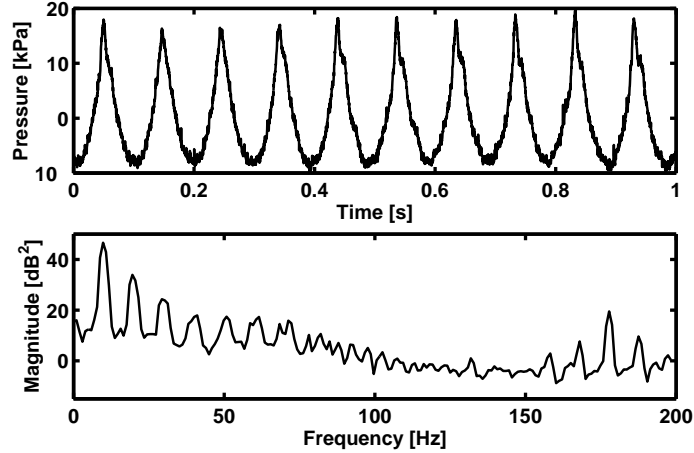


Figure 2: Typical pressure measurements obtained from the floor-mounted pressure transducer during the instability. The signal was low-pass filtered at 2 kHz . Also shown is an average power spectral density obtained from several such signals.

3 Pressure Measurements

To further quantify the instability, pressure measurements were taken using a pressure transducer flush-mounted in the floor of the water tunnel test section, approximately even with the propeller in a streamwise direction and 15 cm below the axis of propeller rotation. A typical signal obtained from the floor-mounted transducer is shown in Figure 2. The signal is clearly periodic, with a frequency corresponding to the frequency of cavitation variation observed visually. The magnitude of the pressure oscillations produced by the instability was as high as $15 - 20\text{ kPa}$, at least one order of magnitude higher than the cavitation noise radiated under stable conditions. These pressure oscillations were strong enough to be readily heard in the laboratory and to shake the test section violently.

Also shown in Figure 2 is an average of several power spectral densities of the pressures generated by the instability. Clearly visible at approximately 10 Hz is the fundamental frequency of the instability, dominating the instability noise by a margin of approximately 15 dB . Many harmonics can also be seen. The blade passage frequency for the six bladed propeller rotating at $n = 30.0\text{ Hz}$ is also clear as are two beat frequencies at 170 Hz and 190 Hz .

As suggested by Huse (1972), the far field pressure from a fluctuating cavity volume will be dominated by the volumetric acceleration imposed upon the flow. Specifically,

$$\tilde{p} \sim \frac{d^2 \tilde{V}_{cav}}{dt^2} \quad (1)$$

where \tilde{p} is the fluctuating far field pressure and \tilde{V}_{cav} is the fluctuating cavity volume. To estimate this volumetric acceleration, high speed video footage similar to that shown in Figure 1 was obtained and synchronized with measurements from the floor-mounted pressure transducer. Frames of the video footage were then digitally captured and analyzed. In each frame, the cavitation extent varied substantially with radial location, but was most easily characterized by the maximum value of a cavity length, l , measured normal to the leading edge. From this cavity length measurement, an estimate of the cavity volume was obtained by following the suggestion of Blake (1986) that $V_{cav} \sim Rl^2$, where R is the propeller radius.

A finite difference method was then applied to the cavity volume estimates to determine the second time derivative of cavity volume and therefore the volumetric acceleration imposed upon the flow. Figure 3 shows the results of this calculation and the comparison with the pressure measurements obtained from the floor-mounted transducer. Note that the qualitative agreement between the two is very good, even in some of the higher frequency details. However, we also note that the vertical scales in Figure 3 have been arbitrarily chosen to facilitate the comparison. As will be seen, quantitative comparison requires detailed knowledge of the response of the facility.

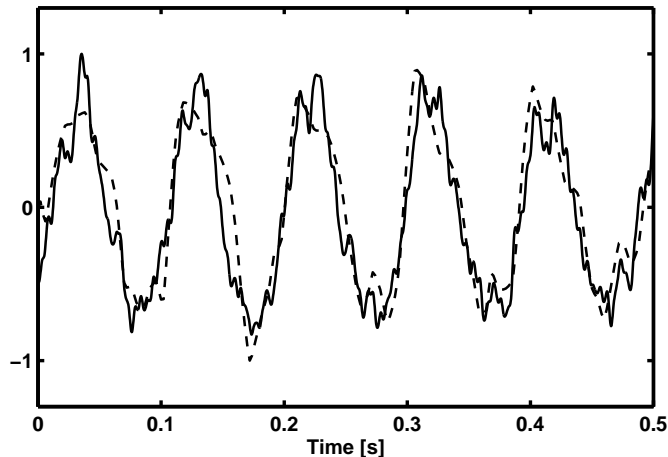


Figure 3: A comparison between the signal from the floor-mounted pressure transducer low-pass filtered at 200 Hz (—) and the second time derivative of the measured cavity volume (---). The vertical scales are arbitrary.

4 Onset of Instability

Figure 4 summarizes the onset of the instability in an advance ratio and cavitation number map. The unstable operating conditions are concentrated at advance ratios, J , below the design advance ratio of $J_o = 1.15$, and at lower cavitation numbers. Some insight regarding the onset of the instability can be gained by considering the following argument. Studies of two-dimensional foils, for example by Tulin (1953) (see also Brennen 1995), have shown that the non-dimensional cavity length, l/c , is essentially a function of the ratio, α/σ , of the angle of attack of the hydrofoil, α , to the cavitation number, σ . Based on purely geometric arguments, the angle of attack in the vicinity of a propeller blade tip is approximately proportional to the difference, $J_o - J$, between the design advance ratio and the operating advance ratio. Thus a particular configuration of cavity lengths on the propeller should correspond to a particular value of the parameter $\xi = (J_o - J)/\sigma$.

Several lines of constant ξ are plotted in Figure 4 where it is clear that the transition between stable and unstable behavior corresponds quite closely to the particular value of $\xi = 2.0$. Thus the instability boundary corresponds to a particular configuration of cavity lengths on the propeller blade. This supports the suggested connection with the partial cavity instability observed on two-dimensional foils, where stability was also related to the ratio of cavity length to chord.

5 Facility Dynamics

To estimate the amplitude of the pressures generated by the instability, a model is needed to describe the response of the entire experimental system to the fluctuating flow rates produced by the cavitating propeller. In developing this model, it is assumed that the facility responds linearly to perturbations in the flow conditions. Accordingly, the quantities of interest are expressed as a linear combination of a mean component and a fluctuating component of frequency ω . The mass flow rate and total pressure are therefore denoted by

$$m = \bar{m} + \text{Re}[\tilde{m}e^{j\omega t}] \quad ; \quad p^T = \bar{p}^T + \text{Re}[\tilde{p}^T e^{j\omega t}] \quad (2)$$

where \bar{m} and \bar{p}^T are the time-averaged mass flow rate and total pressure. The fluctuating components \tilde{m} and \tilde{p}^T are complex, in order to incorporate both the amplitude and phase of the fluctuations.

The dynamics of the facility can be characterized by considering the response of the facility to a fluctuating mass flow rate, \tilde{m}_e , injected at some specific location in the system. We define a system impedance, $Z = \frac{\tilde{p}_e^T}{\tilde{m}_e}$ where, in general, Z is complex, and its value depends on the location of the excitation point.

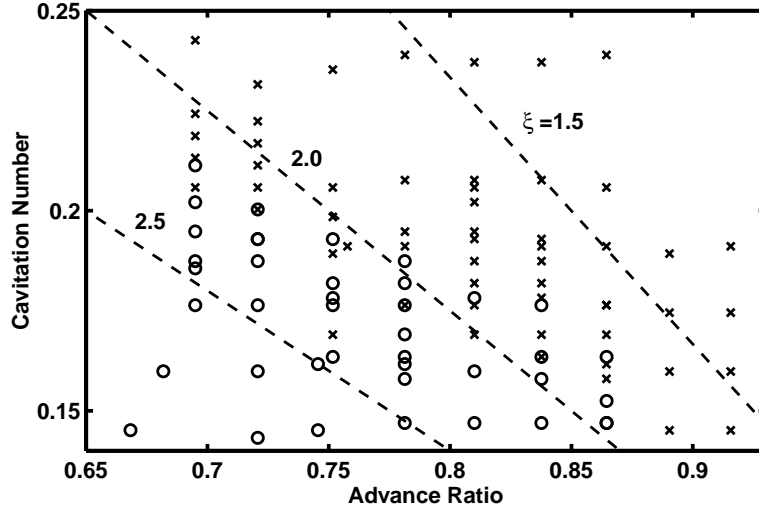


Figure 4: Occurrence of the instability in a cavitation number and advance ratio map. Each operating point is classified as stable (\times), unstable (\circ), or marginally stable (\otimes). The propeller rotation speed in this case was $n = 30.8 \text{ Hz}$. The dashed lines ($-$) are for different values of the parameter ξ , and correspond to the stability criterion discussed in the text.

To develop a specific expression for the system impedance, Z , we employ a lumped parameter approach, dividing the experimental facility into smaller components exhibiting resistive, inertive, and compliant behavior. The details of this analysis are given in Duttweiler (2001). In summary, neglecting resistive behaviors, the facility dynamics are characterized by (1) the compliance, C_{ot} , of the overflow tank that allows control of the pressure within the facility and therefore has the only deliberate free surface, (2) the resistance, R_c , and inertance, L_c , of the pipe leading from the tunnel to this overflow tank, (3) the compliance, C_t , associated with the expansion and contraction of the walls of the tunnel, and (4) the inertances, L_{tu} and L_{td} , associated with the typical upstream and downstream flow paths leading from the point of excitation to the location of the expanding and contracting walls. More specifically, neglecting the resistive components in the system, the impedance at a point of excitation just downstream of the cavitating propeller is given by

$$Z = \frac{j(L_c C_{ot} w^2 - 1)(L_t C_t w^2 - 1)}{w[(L_c + L_t)C_{ot} C_t w^2 - C_{eq}]}, \quad (3)$$

where $L_t^{-1} = L_{tu}^{-1} + L_{td}^{-1}$ and $C_{eq} = C_{ot} + C_t$.

6 Cavitation Dynamics

The facility dynamics captured in Equation 3 demonstrate that the test section flow conditions will respond to the volumetric excitations imposed by a fluctuating cavity volume in the tunnel test section. Yet, the cavity volume itself responds to changes in the test section flow conditions. Clearly then, the cavitation dynamics and facility dynamics must be considered as part of a coupled system.

Essential to understanding these coupled dynamics is determining how the cavity volume responds to changing test section conditions. As described by Brennen (1994), these variations in cavity volume are essentially a function of the upstream pressure, p_t , and mass flow rate, m_t , and can be considered in terms of a cavitation compliance $K = -\rho(dV_{cav}/dp_t)_{m_t}$ and a mass flow gain factor $M = -\rho(dV_{cav}/dm_t)_{p_t}$. It is convenient to recast these dynamic characteristics in terms of the advance ratio, J , and the cavitation number, σ , such that

$$K \doteq -\rho \left(\frac{dV_{cav}}{dp_t} \right)_{m_t} = -\frac{2}{\Omega^2 R^2} \left(\frac{dV_{cav}}{d\sigma} \right)_J ; \quad M \doteq -\rho \left(\frac{dV_{cav}}{dm_t} \right)_{p_t} = -\frac{\pi}{A_t \Omega R} \left(\frac{dV_{cav}}{dJ} \right)_\sigma \quad (4)$$

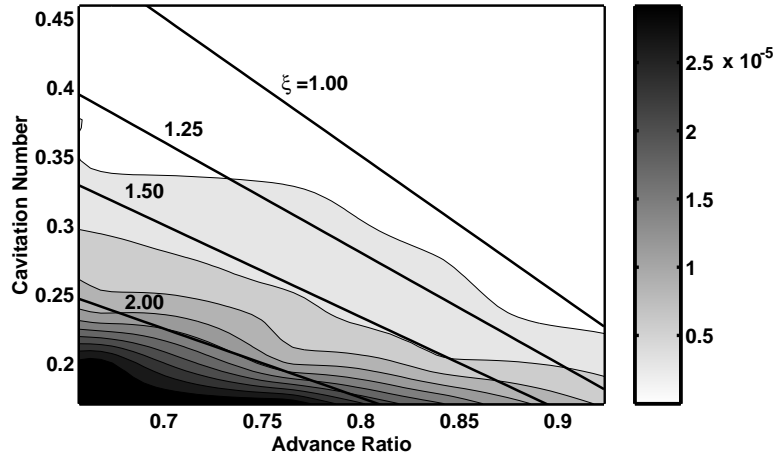


Figure 5: Cavitation volume on propeller blades at intermediate rotation speed ($n = 28.3 \text{ Hz}$). The gray scale on the right indicates the cavitation volume in m^3 . The lines in the map are lines of constant ξ as indicated.

where $\Omega = 2\pi n$ is the radian frequency of the propeller rotation, R is the radius of the propeller, and A_t is the test section cross-sectional area.

It is valuable to determine quasi-static values for K and M using experimental data for the cavity volume as a function of J and σ . Figure 5 shows the results from such a set of experiments. Since the cavity length is essentially a function of the parameter $\xi = (J_o - J)/\sigma$, it follows that the cavity volume will also be a function of this single parameter. Accordingly, several lines of constant ξ are plotted in Figure 5. Then, given the good correspondence between lines of constant ξ and the experimentally determined contours of constant volume, it is convenient to fit the cavity volume to a function of the form $V_{cav} = h(\xi)$. Choosing a second order polynomial $h(\xi) = a\xi^2 + b\xi + c$, Equations 4 yield

$$K = \frac{2}{\Omega^2 R^2 \sigma} (2a\xi^2 + b\xi) \quad ; \quad M = \frac{\pi}{A_t \Omega R \sigma} (2a\xi + b) \quad (5)$$

where $a = 0.86 \times 10^{-5} \text{ m}^3$ and $b = -1.2 \times 10^{-5} \text{ m}^3$.

To facilitate comparison with results obtained by previous investigators exploring the unstable behavior of cavitating pumps, the dynamic cavitation parameters are non-dimensionalized by

$$K^* = \frac{\Omega^2 K}{R} \quad ; \quad M^* = \Omega M \quad (6)$$

It is also necessary to account for the fact that, in the case of a cavitating pump, the mass flow gain factor is based on the mass flow rate entering the cross-sectional area of the pump. In contrast, the definition of Equation 6 is based on the mass flowing through the cross-sectional area of the entire test section. For appropriate comparison, an adjustment is necessary, increasing the mass flow gain factor computed for the propeller by a factor of $\eta = A_t/A_x$, the ratio of the test section area to the area of the propeller disc.

After this adjustment, the ranges of the dimensionless cavitation compliance and dimensionless mass flow gain factor are determined to be $K^* = 0.0 - 1.4$ and $M^* = 0.05 - 0.20$ for the advance ratios and cavitation numbers investigated at $n = 28.3 \text{ Hz}$. At $n = 31.7 \text{ Hz}$, these ranges increase slightly to $K^* = 0.0 - 1.6$ and $M^* = 0.0 - 0.4$. For comparison, in the first estimate of these dynamic parameters for a cavitating inducer, Brennen (1976) obtained values in the ranges of $K^* = 0.05 - 0.2$ and $M^* = 0.6 - 0.8$ for cavitation numbers above $\sigma = 0.02$. Experimental measurements by Brennen *et al.* (1982) for cavitating inducers at $\sigma = 0.2$ yielded a larger typical value of $K^* = 0.25$, but similar values of $M^* = 0.6$. More recently, theoretical studies by Otsuka *et al.* (1996) examined the potential frequency dependence of K^* and M^* . At low frequencies and $\sigma = 0.17$, they obtained values of the order of $K^* = 0.06$ and $M^* = 0.6$. All of these values are in reasonable agreement with the current work, since differences would be expected given the geometrical differences between propellers and pumps.

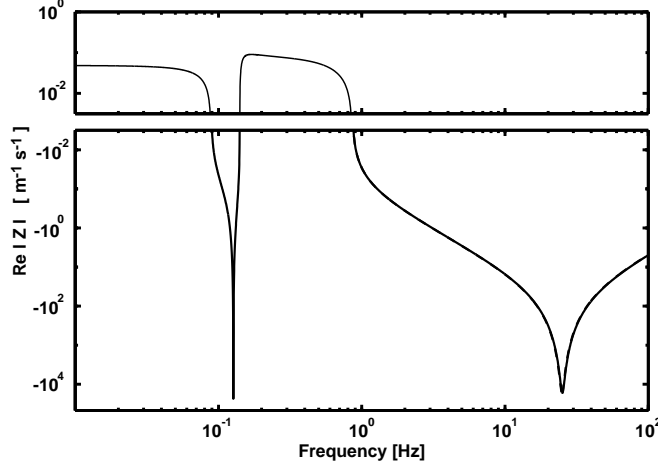


Figure 6: Real part of system impedance, Z , for the combined facility and cavitation dynamics model of Equation 8.

7 Facility and Cavitation Dynamics

The inclusion of the cavitation dynamics significantly alters the character of the overall system dynamics. The nature of this change is most clearly illustrated by considering a simplified system consisting only of a source of fluctuating mass flow rate and the cavitation dynamics discussed in section 6. If the outlet of the propeller is assumed closed to fluctuations in mass flow rate, then the impedance of this system is given by

$$Z = \frac{1 - j\omega M}{j\omega K} \quad \text{and} \quad \text{Re}[Z] = -\frac{M}{K} \quad (7)$$

Equations 5 and Figure 5 indicate that the cavitation compliance and mass flow gain factor are both positive. Therefore, this simplified system is characterized by a negative value of the real part of the system impedance, $\text{Re}[Z]$. Accordingly the system is an active one in that it is capable of sustaining fluctuations without an external input of fluctuation energy, instead extracting the fluctuation energy from the steady flow. This is in accord with the view of other investigators such as Brennen (1978) and Tsujimoto *et al.* (1993) who characterize cavitating pump instabilities as essentially arising from a positive mass flow gain factor.

The effects of this behavior on a more complete model incorporating both the facility and cavitation dynamics can be seen by modifying the model of Equation 3 to include the cavitation dynamics. The system impedance at a point just downstream of the cavitating propeller is then given by

$$Z = \frac{(L_t C_t \omega^2 - 1) Z_c}{j L_t C_t \{Z_c K - M\} \omega^3 - L_t C_t \left\{ \frac{Z_c M}{L_{tu}} - 1 \right\} \omega^2 + j \{M - Z_c (C_t + K)\} \omega - 1} \quad (8)$$

where $L_t^{-1} = L_{tu}^{-1} + L_{td}^{-1}$, and Z_c is the impedance of the connecting pipe and overflow tank, $Z_c = j\omega L_c + 1/j\omega C_{ot}$.

Figure 6 plots the real part of this system impedance as a function of frequency. In generating this plot, values of $K = 5.9 \times 10^{-6} \text{ m.s}^2$ and $M = 5.9 \times 10^{-4} \text{ s}$ were obtained from Equation 5. The value for the tunnel compliance, $C_t = 5 \times 10^{-3} \text{ m.s}^2$, was determined based on facility natural frequency experiments described in Duttweiler (2000). The value of the overflow tank compliance, C_{ot} , was calculated based on the reduced overflow tank pressure, $p_{ot} = 18 \text{ kPa}$, required to obtain cavitating conditions. The remaining parameters were evaluated from the physical dimensions of the experimental facility.

Immediately apparent from Figure 6 is that the real part of the system impedance is negative over two frequency ranges centered at approximately $f = 0.12 \text{ Hz}$ and $f = 25 \text{ Hz}$. The active nature of the cavitation dynamics exemplified by Equation 7 is still evident, but with the addition of the facility dynamics the positive activity has been limited to these two frequency ranges.

The unstable region around 0.12 Hz corresponds to the natural frequency of the experimental facility, detailed in Duttweiler (2000). The trough at $f = 25 \text{ Hz}$ therefore seems a probable explanation for the propeller instability. At this frequency, the combination of facility and cavitation dynamics results in the creation of fluctuation energy and therefore potentially unstable behavior of the cavitation on the propeller.

However, there is a large discrepancy between the frequency of this trough and the typical experimentally observed instability frequency of $f = 10 \text{ Hz}$. This is possibly attributable to the fact that the estimate of the cavitation compliance used in determining the frequency is based only on the cavity volume variation observed on the propeller blades. If an estimate is made to include the effects of the cavity volume variation within the tip vortices (Duttweiler 2001), the cavitation compliance may be increased by as much as a factor of six. This increase in cavitation compliance results in an instability frequency of $f = 10.4 \text{ Hz}$. Another possibility is that non-linear effects produce a limit cycle frequency which is significantly smaller than the prediction of the linear instability analysis.

8 Conclusions

This paper has described an investigation of a previously unreported surge instability on a cavitating propeller mounted in a water tunnel. The cyclic behavior of the attached blade cavities has strong similarities to that of partial cavity oscillation on single hydrofoils in that the cavity length oscillates between a configuration in which the length is substantially less than the chord over almost all of the span and one in which a significant fraction of the cavity near the tip is longer than the chord. The reduced frequency of the instability is consistent with the partial cavity instability on single foils. The amplitudes of the pressures generated are large and potentially damaging to the surrounding structure.

To understand the nature of this instability and its source, separate investigations of the cavitation dynamics and of the response of the water tunnel were undertaken. It is demonstrated that the cavitation dynamics may be characterized by an approach previously deployed during identification of the dynamics of cavitating pumps; quasi-static observations of the parametric variations in the cavity volume are then used to quantify the quantities known as the cavitation compliance and the mass flow gain factor.

Through combination of these dynamics with a previously determined dynamic response of the water tunnel to volumetric oscillations created by means of a piston device, a complete model of the linear cavitation and facility dynamics is then constructed. This model demonstrates that the instability is essentially driven by a positive mass flow gain factor. It predicts instability characteristics (frequencies, etc.) which are mostly in accord with the observations. However, some features of the instability remain unexplained, such as the role of the supporting strut asymmetry; these may be a consequence of unidentified dynamic features of the water tunnel.

Whether or not the instability could occur in the environment downstream of a ship hull would require the construction and analysis of a dynamic model which included both the cavitation characteristics utilized herein as well as a model for the response of the surroundings to the volume oscillations. While the literature contains a number of attempts to model the surroundings (see, for example, Huse 1972, Weitendorf 1989) the authors do not know of any complete model of the type suggested here.

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