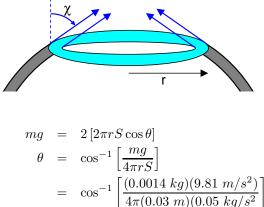
Solution to Problem 108C

A soap bubble hangs from a horizontal circular ring of radius r equal to 3cm. The mass of the soapy water comprising the bubble is $m = .0014 \ kg$. It is assumed that the bubble is spherical and any contact angle effects at the junction of the ring are negligible.

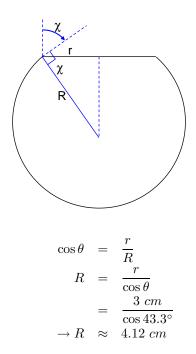
[1] The weight of the soap film must balance the component of the surface tension force, S. Note that there are two surfaces to consider.



$$= \cos^{-1} \left[\frac{(0.0014 \ kg)(9.81 \ m/s)}{4\pi (0.03 \ m)(0.05 \ kg/s)} \right]$$

$$\to \theta \approx 43.3^{\circ}$$

[2] The radius of the soap bubble follows from the geometry:



[3] The thickness of the soap bubble follows from the density of the soapy water ($\rho = 1000 \ kg/m^3$) and the mass (m =.0014 kg). By assuming $t \ll R$, the approximate volume is given by the (surface area)×(thickness). The surface area follows from integration:

$$A(\theta) = 2\pi R^2 \int_{-\pi/2}^{\theta} \cos\phi \ d\phi$$

$$= 2\pi R^{2} (1 + \sin \theta)$$

$$\therefore m = \rho V \approx \rho A(\theta) t$$

$$\to t = \frac{m}{\rho A(\theta)} = \frac{0.0014 \ kg}{(1000 \ kg/m^{3})(2\pi)(0.0412 \ m)^{2}(1 + \sin(43.3^{\circ}))}$$

$$t = 7.78 \times 10^{-5} \ m$$