Problem 205C

A circular air-cushion vehicle of weight, W, uses a fan to pressurize the air cushion and thus elevate the vehicle:



For simplicity we assume that the air has a constant and uniform density, ρ . The fan characteristic is such that the pressure rise, $p_c - p_a$ (where p_c and p_a are the pressures in the cushion and the surrounding atmospheric pressure respectively) is related to the volume flow rate, Q, by

$$p_c - p_a = A - BQ$$

where A and B are known constants. The vehicle is elevated so that a gap, h, is created between the edge of the vehicle and the ground. Find h in terms of W, ρ , A, B and R, the radius of the base of the vehicle. Assume that the loss coefficient for the flow through the gap, h, is unity based on the velocity of the air flow through this orifice.