Solution to Problem 114B:

From the given expressions:

$$\frac{\partial u}{\partial x} = \frac{6x^2yz - 2y^3z}{(x^2 + y^2)^3} \tag{1}$$

and

$$\frac{\partial v}{\partial y} = \frac{-6x^2yz + 2y^3z}{(x^2 + y^2)^3}$$
(2)

and

$$\frac{\partial w}{\partial z} = 0 \tag{3}$$

Therefore

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0 \tag{4}$$

and therefore since the divergence of the velocity is zero the fluid is incompressible.