## Problem 109D:

A constant and uniform layer of Newtonian, viscous, incompressible liquid (dynamic viscosity,  $\mu$ , and density,  $\rho$ ) flows down a flat plate inclined at an angle,  $\theta$ , to the horizontal:



The thickness of the layer is h and the flow is planar with velocity components as follows:

$$u_n = 0 ; u_s(n) = Cn(2h-n)$$
 (1)

where C is a constant. Find:

- [a] An expression for C in terms of  $\rho$ ,  $\mu$ ,  $\theta$  and the acceleration due to gravity g.
- [b] The pressure acting on the plate if the atmospheric pressure is denoted by  $p_a$ .